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Improved line strengths of rovibrational and rotational transitions within the $X^3\Sigma^-$ ground state of NH

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Recently, a line list including positions and transition strengths was published for the NH $X^3\Sigma^-$ rovibrational and rotational transitions. The calculation of the transition strengths requires a conversion of transition matrix elements from Hund's case (b) to (a). The method of this conversion has recently been improved during other work on the OH $X^2\Pi$ rovibrational transitions, by removing an approximation that was present previously. The adjusted method has been applied to the NH line list, resulting in more accurate transition strengths. An updated line list is presented, that contains all possible transitions with v' and v'' up to 6, and J up to between 25 and 44, depending on the band.

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I. INTRODUCTION

We recently published line lists, including positions and transition strengths, for the NH $X^3\Sigma^-$ state rovibrational and rotational transitions¹. The calculation of the transition strengths involved an approximation (see Section II), but the method has since been improved (in our OH $^2\Pi$ work²) and this approximation removed, resulting in a more accurate distribution of intensity between different spin-component transitions. The previously published NH transition strengths are already in use, and as a single adjustment to the calculations can result in an improvement in the transition strengths, we believe that it is important to provide an updated list.

NH is an important molecule in astronomy, as its transitions have been used to calculate the nitrogen abundance in the Sun^{3,4} and other stars^{5–8}, and it has also been detected in comets⁹ and diffuse interstellar clouds^{10–13}. Other areas in which its transitions are useful are those of combustion science^{14,15} and magnetic trapping^{16–23}, which has applications to fields such as quantum computing²⁴ and high precision spectroscopy^{25,26}. Use of the previous line list could result in slightly inaccurate NH and nitrogen abundances being obtained in astronomical and combustion environments, and we would like to direct potential users to the updated list presented in this note.

II. CALCULATION METHOD

The calculation method will briefly be described here, but for a full description, see refs. [1] and [27]. Molecular constants are obtained from fits to available experimental line positions, and equilibrium constants are determined from fits to the molecular constants G_v and B_v . A potential energy curve (PEC) is calculated using the program RKR1²⁸, which takes the equilibrium constants as input. The PEC and dipole moment function (DMF) (from refs. [18] and [1]) are then entered along with a dissociation energy (DE) into the program LEVEL²⁹. The DE used is $27176 \pm 280 \text{ cm}^{-1}$ from the theoretical calculations of Espinosa-García *et al.*³⁰. This compares well with a range of experimental values that they reported (26535.91 - $27987.396 \text{ cm}^{-1}$ ^{31–33}), and with another theoretical value of $27181 \pm 242 \text{ cm}^{-1}$ ³⁴. LEVEL extrapolates the PEC (using the DE as a limit), and calculates vibrational wavefunctions and then transition matrix elements (MEs) between the relevant states. These

MEs include the Herman Wallis (H-W) effect (vibration-rotation interaction). Finally, PGOPHER³⁵ takes the molecular constants and MEs as input, and calculates transition strengths in the form of Einstein A values.

LEVEL does not include electron spin, and its MEs are in terms of N and not J , and we describe these as Hund's case (b) MEs. The calculations in PGOPHER use a case (a) basis, and so the MEs from LEVEL need to be converted from case (b) to (a) before entry into PGOPHER. A

TABLE I. Transition matrices for the (1,0), R(4) transition, when the old transformation equation (TE) is used. Left: e parity matrix, right: transformed matrix in terms of the real states. All values are in debye.

	$J'=5$	$J'=5$		$J'=5$	$J'=5$
	$\Sigma=\pm 1$	$\Sigma=0$		F_{1e}	F_{3e}
$J=4$	-0.148372	0	$J=4$	-0.149797	0.000122
$\Sigma=\pm 1$			F_{1e}		
$J=4$	0	-0.151539	$J=4$	0.003031	-0.150099
$\Sigma=0$			F_{3e}		

TABLE II. Same as Table I, but when the new TE is used.

	$J'=5$	$J'=5$		$J'=5$	$J'=5$
	$\Sigma=\pm 1$	$\Sigma=0$		F_{1e}	F_{3e}
$J=4$	-0.148372	0.004912	$J=4$	-0.144421	0.0000992
$\Sigma=\pm 1$			F_{1e}		
$J=4$	0.005897	-0.151539	$J=4$	0.002024	-0.155484
$\Sigma=0$			F_{3e}		

transformation equation (TE) to perform this conversion was derived in the CN work²⁷, with the full derivation shown in the appendix to that paper.

The TE was revisited in more recent work on the $X^2\Pi$ state of OH, where it was found that the transformation of the vibronic transition moment to the case (a) basis introduced small $\Delta\Sigma \neq 0$ MEs. This is unexpected for an electric dipole transition, and is a consequence of the N dependence of the vibronic transition dipole. As shown in ref. [2], if the dipole

is independent of N (i.e. in the absence of the H-W effect) the $\Delta\Sigma \neq 0$ MEs are zero as expected for Hund's case (a). (Note that this effect is distinct from the standard Hund's case (a)/case (b) mixing, which is already accounted for.) The revised TE is:

$$\begin{aligned}
& \langle \eta' \Lambda'; S \Sigma' | T_{\Omega' - \Omega}^k(\mu, J' \Omega' J \Omega) | \eta \Lambda; S \Sigma \rangle = \\
& (-1)^{J' - \Omega'} \begin{pmatrix} J' & k & J \\ -\Omega' & \Omega' - \Omega & \Omega \end{pmatrix}^{-1} \\
& \times \sum_{N, N'} (-1)^{N' - N + \Omega' - \Omega + S + J + \Lambda' + k} (2N' + 1)(2N + 1) \\
& \times \begin{pmatrix} J' & S & N' \\ \Omega' & -\Sigma' & -\Lambda' \end{pmatrix} \begin{pmatrix} J & S & N \\ \Omega & -\Sigma & -\Lambda \end{pmatrix} \begin{Bmatrix} N' & J' & S \\ J & N & k \end{Bmatrix} \\
& \times \begin{pmatrix} N' & k & N \\ -\Lambda' & \Lambda' - \Lambda & \Lambda \end{pmatrix} \langle \eta' \Lambda' | T_{\Lambda' - \Lambda}^k(\mu, N' N) | \eta \Lambda \rangle.
\end{aligned} \tag{1}$$

where η represents the remaining electronic and vibrational quantum numbers, k is the rank of the tensor (equal to 1 for single photon transitions), and $T_{\Omega' - \Omega}^k(\mu, J' \Omega' J \Omega)$ and $T_{\Lambda' - \Lambda}^k(\mu, N' N)$ are the molecule fixed electric dipole operators in spherical tensor notation. For a more detailed description of the changes to the TE, see our recent OH work and its supplementary material². The effect of the change is that small $\Delta\Sigma \neq 0$ MEs appear in the Hund's case (a) transition matrices. For example, for the (1,0) R(4) transition, the case (a) symmetrized transition matrix set up by PGOPHER when the old version of the TE is used is that shown in the left panel of Table I. This matrix is then combined in PGOPHER with the eigenvectors resulting from the diagonalization of the Hamiltonian matrices, to produce the MEs in terms of the real states, as shown in the right panel of the table. Only the e parity matrix is shown, as the f parity matrix consists of only one element ($\Sigma = \pm 1$), and is unaffected by the change in the TE as there are no $\Delta\Sigma \neq 0$ MEs. When the adjusted TE is used, the off-diagonal MEs appear as in the left panel of Table II, and the final MEs are those shown in the right panel.

The calculations have been performed using the same molecular constants, PEC, DMF, and methods as in the previous work, but with use of the adjusted TE to convert the transition MEs from case (b) to (a), from the output of LEVEL to the input of PGOPHER.

The line list has been updated, and contains all possible transitions with v' and v'' up to 6, and J up to between 25 and 44, depending on the band. The vibrational band Einstein

$A_{v'v}$ and $f_{v'v}$ values have also been updated. $A_{v'v}$ values are equal to the sum of $A_{J'J}$ values for transitions between v' and v , with $J'=1$ (an average of the three F' values is taken)³⁶. $f_{v'v}$ values were then calculated using the same method as in the previous work¹. The line list, molecular constants, ab initio DMF, PEC, Einstein $A_{v'v}$ and $f_{v'v}$ values, and PGOPHER input file (which can be used to view all transition MEs) are available in the supplementary material³⁷.

III. ANALYSIS

The H-W effect causes the R branches to be much stronger than the P branches, and the ratio of R branch to P branch intensity for the same upper N level (H-W ratio) varies with N . As these ratios use the same upper N levels (for comparison with an emission spectrum), the effects of level population are canceled, and so they are useful for the comparison of observed and calculated intensity ratios.

Each $N'-N$ transition is mainly made up of three fine structure $J'-J$ transitions, with $F'=F''$. The main effect of the inclusion of $\Delta\Sigma \neq 0$ MEs on a particular $N'-N$ transition, is a small redistribution of intensity between the different possible $J'-J$ transitions. The observed spectrum was not of high enough resolution to resolve the fine structure adequately for intensity measurements, and instead the sum of the fine structure transitions was used to calculate the H-W ratios for comparison with the calculated values. The redistribution of intensity therefore has little effect on the calculated ratios, so unlike in our OH work, we cannot offer any experimental validation of the updated transformation, though the agreement with the sum remains good.

Figure 1 shows the change in transition strengths resulting from the change in the transformation, using the (1,0) band as an example. The general trend is that transitions with the same N value now have a smaller range of A values than they did with the original TE. The A values become closer with increasing N , so that by $N'=8$ they are almost identical. Despite this, the lines within a triplet in the spectrum will still have noticeably different transition strengths, as the levels involved have different values of J , and therefore different degeneracies.

For the pure rotational transitions, the effect of the adjusted TE is less than for the rovibrational transitions. At low N , the A values are very similar for both equations, though

FIG. 1. Einstein A values for the three strong components of the (1,0) band P branch with the two different TEs. A single curve shows for the F_{22} transitions, as they are not affected by the type of transformation.

they diverge slightly with increasing N .

The change in Einstein A generally increases with decreasing transition strength, with a maximum change of about six orders of magnitude. The large changes only occur for transitions that are so weak that they are unlikely to ever be observed, most of which are high Δv or satellite transitions. The largest change for any transition that has previously been observed is about 18%, with most below 4%.

IV. CONCLUSION

It has been shown that it is possible to improve part of the method used to calculate a previous NH $X^3\Sigma^-$ line list of positions and transition strengths. The calculations have been repeated (Section II), and an updated line list has been provided in the supplementary material³⁷. This will be useful in fields such as astronomy, combustion science, and magnetic trapping, and will enable the calculation of more accurate NH and nitrogen abundances compared to the previous list.

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